

Analysis  
Supplementary problems  
Complex numbers

**Exercise 1.** Put under the polar form, the following complex numbers:

•

$$z_1 = 2 + 3i$$

,

•

$$z_2 = -3i$$

,

•

$$z_3 = -\sqrt{6} - i\sqrt{2}$$

.

**Exercise 2.** :

1. Find  $x$  and  $y$  such that

$$3x + 2i - ix + 5y = 7 + 5i. \quad (1)$$

2. Put under the form  $x + iy$

1.

$$\frac{2 + i}{3 - 2i}, \quad (2)$$

2.

$$(1 + i)^n + (1 - i)^n, \quad n \in \mathbb{N}. \quad (3)$$

**Exercise 3.** Resolve the following equations:

1.

$$z^3 = -1,$$

2.

$$z^2 = -8 + 6i.$$

**Exercise 4.** Describe the following sets:

•

$$A = \{z \in \mathbb{C} : |z + 1| \leq 1\} \quad (4)$$

•

$$A = \{z \in \mathbb{C} : \frac{|z + 1|}{|z - 1|} = 1\} \quad (5)$$