

## **A suggested course of Master**

**Presented by Dr. Bradji, Abdallah**

**Title: Finite Volume Method for PDEs**

**Remark: the following programme is provisional. Changes will be made according to the time and background of students. Changes will also made according to the other suggested courses.**

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### **Contents :**

#### **1 Introduction 4**

- 1.1 Examples
- 1.2 The finite volume principles for general conservation laws .
  - 1.2.1 Time discretization
  - 1.2.2 Space discretization
- 1. Comparison with other discretization techniques

#### **2 A one-dimensional elliptic problem**

- 2.1 A finite volume method for the Dirichlet problem
  - 2.1.1 Formulation of a finite volume scheme
  - 2.1.2 Comparison with a finite difference scheme
  - 2.1.3 Comparison with a mixed finite element method
- 2.2 Convergence theorems and error estimates for the Dirichlet problem
  - 2.2.1 A finite volume error estimate in a simple case
  - 2.2.2 An error estimate using finite difference techniques
- 2.3 General 1D elliptic equations
  - 2.3.1 Formulation of the finite volume scheme
- 2. Error estimate

#### **3 Elliptic problems in two or three dimensions**

- 3.1 Dirichlet boundary conditions
  - 3.1.1 Structured meshes
  - 3.1.2 General meshes and schemes
  - 3.1.3 Existence and estimates
  - 3.1.4 Convergence
  - 3.1.5  $C_2$  error estimate

## **4 Parabolic equations**

4.1 Meshes and schemes

4. Error estimate for the linear case

## **5 Hyperbolic equations in the one dimensional case**

5.1 The continuous problem

5.2 Numerical schemes in the linear case

5.2.1 The centered finite difference scheme

5.2.2 The upstream finite difference scheme

5. The upwind finite volume scheme

## **6 Multidimensional nonlinear hyperbolic equations**

6.1 The continuous problem

6.2 Meshes and schemes

6.2.1 Explicit schemes

6.2.2 Implicit schemes

6. Passing to the limit

## **Reference**

**EMARD, R., GALLOUET, T. & HERBIN, R. (2000) Finite volume methods. Techniques of Scientific Computing, Part III, Handbook of Numerical Analysis (P. G. Ciarlet & J.-L. Lions eds), vol. VII. Amsterdam: North-Holland, pp. 713–1020**