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Fast dictionary-based approach for mass spectrometry data analysis

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Joint work	with				





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Motivation

Mass Spectrometry (1/2)

■ Mass Spectrometry :

• A technique used to measure the characteristics, the chemical composition and the structure of a sample or molecule.

• 1919, Joseph John Thomson.

■ Utility area :

• Pharmaceutical : drug discovery, combinatorial chemistry, pharmacokinetics, drug metabolism.

- Clinical : neonatal screening, haemoglobin analysis, drug testing.
- Environmental : water quality, food contamination.
- Geological : oil composition.
- Biotechnology : analysis of proteins, peptides.



Principle of measure :



■ Aim : Analyse efficiently big MS data.

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Outline

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- Observation model
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- Optimization strategy
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- Practical Implementation
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Problem statement

Some reminders on chemistry

Atom ?

- Atomic number = Number of protons.
- Mass number = Number of protons + neutrons.

Molecule ?

Set of atoms linked together.

Isotopic pattern ?

An atom can be present under different forms with different numbers of neutron, called **isotopes**.

Each stable isotope is present in the nature with a specific **abundance**.

Atomic Structure



Protein class (1/2)

$\blacksquare \text{ Protein formula } (C_{\textit{N}_{C}}H_{\textit{N}_{H}}O_{\textit{N}_{O}}N_{\textit{N}_{N}}S_{\textit{N}_{S}})$

Atom Name	Atom Symbol	Mass (in Dalton)	Relative Abundance
Carbon	¹² C	12 (by definition)	0.9893
Carbon	¹³ C	13.0033548378	0.0107
Hydrograp	¹ H	1.00782503207	0.999885
nyurogen	² H	2.0141017778	0.000115
	¹⁶ O	15.99491461956	0.99757
Oxygen	¹⁷ 0	16.99913170	0.00038
	¹⁸ O	17.9991610	0.00205
Nitrogon	¹⁴ N	14.0030740048	0.99636
Nitrogen	¹⁵ N	15.0001088982	0.00364
	³² S	31.97207100	0.9499
Sulfur	³³ S	32.97145876	0.0075
	³⁴ S	33.96786690	0.0425

Isotopic mass and natural abundance of atoms found in proteins (by definition)



 \rightsquigarrow The larger the molecule, the larger is the number of different isotopes present, associated with specific probabilities of appearance.

How to find the position of the mono-isotopic peak from a large pattern distribution?

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Observation model

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Mathematical model

For a given chemical sample, composed of P different molecules with monoisotopic mass $m_p^{\text{iso}} \in (0, +\infty)$, charge state $z_p \in \mathbb{N}^*$ and abundance $a_p \in (0, +\infty)$, for $p \in \{1, \ldots, P\}$:

$$y = \sum_{p=1}^{P} a_{p} D(m_{p}^{\text{iso}}, z_{p}) + n$$
 (1)

- y : acquired MS spectrum.
- $D(m_p^{iso}, z_p)$: mass distribution associated to monoisotopic mass m_p^{iso} and charge state z_p .
- n : acquisition noise.
 - Discrete measurements on a grid with size M :

$$\mathbf{y} = \sum_{p=1}^{P} \frac{a_p \mathbf{d}(m_p^{\text{iso}}, z_p) + \mathbf{n}$$
 (2)

with $\mathbf{y} \in \mathbb{R}^{M}$, $\mathbf{d}(m_{p}^{\text{iso}}, z_{p}) \in [0, +\infty[^{M} \text{ and } \mathbf{n} \in \mathbb{R}^{M}.$

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Dictionary-based strategy

Protein molecule : Averagine model [Senko et al., 1994]

$$\begin{array}{cccc} \mathcal{A}: & \mathbb{R}_+ \times \mathbb{N}^* & \to & \mathbb{R}_+ \\ & & (m,z) & \to & \mathbf{d}(m,z) \end{array}$$
 (3)

For *M* candidate values of isotopic masses and *Z* candidate charge values, we define a grid with size T = MZ, and we define the dictionary $\mathbf{D} \in \mathbb{R}^{M \times T}$:

$$\mathbf{D} = \left[\mathbf{D}_{1 \le j \le M, 1}, \mathbf{D}_{1 \le j \le M, 2}, \dots, \mathbf{D}_{1 \le j \le M, T}\right]$$
(4)

• *i*-th column of **D** determined by the averagine model at *i*-th grid position :

$$(\mathsf{D})_{1\leq j\leq M,i}=\mathsf{d}(m_i,z_i)$$

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Problem

$$y = D\overline{x} + n'$$

(5)

where $\mathbf{y} \in \mathbb{R}^{M}$, $\mathbf{D} \in \mathbb{R}^{M \times T}$, $\overline{\mathbf{x}} \in \mathbb{R}^{T}_{+}$ and $\mathbf{n}' \in \mathbb{R}^{M}$.

🗡 y : measure.

- X D : large scale ill-conditioned matrix.
- X T = MZ : very large size.
- \mathbf{X} $\mathbf{\bar{x}}$: unknown sparse vector with positive entries.
- X n' : high noise level.

\Rightarrow III-posed inverse problem in high dimensions.



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Optimization strategy

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Variational formulation

$$\underset{\mathbf{x} \in \mathbb{R}^{\mathcal{T}}}{\operatorname{minimize}} \Phi(\mathbf{x}) \quad \text{subject to} \quad \|\mathbf{D}\mathbf{x} - \mathbf{y}\| \leq \eta$$
(7)

• $\Phi : \mathbb{R}^T \mapsto] - \infty, +\infty]$ is a proper, lower semicontinuous (lsc), convex regularization function used to enforce positivity and sparsity on the solution.

• $\eta > 0$ is a parameter that depends on the noise characteristics.

Proximity operator

Let $\Phi : \mathbb{R} \to] - \infty, +\infty$] a lsc proper and convex function. The proximity operator of Φ is defined as [Moreau, 1965] http://proximity-operator.net/ [Cherni et al., 2017] :

$$\operatorname{prox}_{\Phi}(x) : \mathbb{R}^{\mathbb{N}} \to \mathbb{R}^{\mathbb{N}}$$
$$x \to \operatorname{argmin}_{y \in \mathbb{R}^{\mathbb{N}}} \left(\Phi(y) + \frac{1}{2} \|y - x\|^2 \right)$$

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Primal Dual algorithm [Chambolle and Pock, 2011]

Initialisation $\mathbf{u}^{(0)} \in \mathbb{R}^{M}, \mathbf{x}^{(0)} \in \mathbb{R}^{T}$ $0 < \sigma < \|\mathbf{D}\|^2 / \tau$ $\rho \in (0, 2), \tau > 0$ Minimisation For k = 0, 1, ... $\tilde{\mathbf{x}}^{(k)} = \operatorname{prox}_{\tau \Phi} (\mathbf{x}^{(k-1)} - \tau \mathbf{D}^{\mathsf{T}} (\mathbf{u}^{(k-1)}))$ $\mathbf{v}^{(k)} = \mathbf{u}^{(k-1)} + \sigma \mathbf{D}(2\tilde{\mathbf{x}}^{(k)} - \mathbf{x}^{(k-1)})$ $\tilde{\mathbf{u}}^{(k)} = \mathbf{v}^{(k)} - \sigma \operatorname{proj}_{\parallel -\mathbf{v} \parallel \leq n} (\mathbf{v}^{(k)} / \sigma)$ $\mathbf{x}^{(k)} = \mathbf{x}^{(k-1)} + \rho(\mathbf{\tilde{x}}^{(k)} - \mathbf{x}^{(k-1)})$ $\mathbf{u}^{(k)} = \mathbf{u}^{(k-1)} + \rho(\tilde{\mathbf{u}}^{(k)} - \mathbf{u}^{(k-1)})$

For every $(\mathbf{y}, \mathbf{v}) \in (\mathbb{R}^N)^2$: $\operatorname{proj}_{\|\cdot-\mathbf{y}\| \leq \eta}(\mathbf{v}) = \mathbf{v} + (\mathbf{v} - \mathbf{y}) \min\left(\frac{\eta}{\|\mathbf{v} - \mathbf{y}\|}, 1\right) - \mathbf{y}.$ (8) The convergence of the iterates $(\mathbf{x}^{(k)})_{(k \in N)}$ is ensured [Chambolle and Pock, 2011].

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Practical Implementation

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Dictionary construction

Given a range of masses $[m_{\min}, m_{\max}]$ and charges $[z_{\min}, z_{\max}]$, we define a regular grid :

$$(\forall i \in \{1, ..., T\}) \quad m_i = m_{\min} + (j-1)m_{\max}, \qquad (9) \\ z_i = z_{\min} + (\ell - 1)z_{\max}, \qquad (10)$$

with the convention $i = \ell M + j$, $j \in \{1, \ldots, M\}$ and $\ell \in \{1, \ldots, Z\}$.

The *i*-th column of D is taken as d(m_i, z_i).
d(m_i, z_i) corresponds to a sampled version of D(m, z) on the mass grid with size M.



Circulant approximation

Difficulty

× Very large value for MZ.

 \Rightarrow Large dictionary D which presents a computational challenge

and large memory resources.

Assumptions

• Similar isotopic mass patterns mainly differ by a sample shift of peaks positions.

• Isotopic patterns are sparse with positives entries.

Proposal

 \sim Decompose the mass axis into windows with width $L \leq M$.

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Circulant approximation

Initial dictionary

$$\mathbf{D} = \begin{bmatrix} \mathbf{D}_{1 \le j \le M, 1}, \mathbf{D}_{1 \le j \le M, 2}, \dots, \mathbf{D}_{1 \le j \le M, T} \end{bmatrix} \quad T = MZ$$
(11)

$$\mathbf{D} = \left[\mathbf{D}_1 | \dots | \mathbf{D}_\ell | \dots | \mathbf{D}_Z\right]_{1 \le \ell \le Z}$$
(12)

Circulant model

Each \mathbf{D}_{ℓ} is approximated by the following block diagonal (BDiag) matrix made of M/L blocks assumed to be circulant (Circ) matrices with first line $\overline{\mathbf{d}}_{s,\ell}$, $s \in \{1, \dots, M/L\}$: $\overline{\mathbf{D}}_{\ell} = BDiag\left(\left[\operatorname{Circ}\left(\overline{\mathbf{d}}_{s,\ell}\right)\right]_{1 < s < M/L}\right).$ (13)

✓ Fast computation of products (D, D^T) using fast Fourier tools. ✓ High reduction of the memory requirements.

$$\overline{\mathbf{D}} = \left[\overline{\mathbf{D}}_1 | \dots | \overline{\mathbf{D}}_\ell | \dots | \overline{\mathbf{D}}_Z\right]_{1 \le \ell \le Z}$$
(14)

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Application



Synthetic results (1/4)

Simulated data

Signal A :

• P = 50 proteins





Synthetic results (2/4)

Parameters dataset : Gaussian noise, iid with std $\sigma = 10^{-2}$, $\tau = \theta \sigma \sqrt{M}$, $\theta \simeq 1$.

Parameters algorithm : $\rho = 1.9$, $\tau = ||\mathbf{D}||^{-1}$, $\sigma = 0.9\tau$, maximum iterations number=1000.



Reconstruction results of the signal A : (top) input data y, (bottom) exact spectrum (dots), restored spectrum with exact dictionary (dashed line), and with its block-circulant approximation for L = 10 (asterisks).

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Synthetic results (3/4)

Impact of noise? Memory storage?

σ	Exact dictionary approach		Block-circulant approximation			
0	SNR	Time	Memory storage	SNR	Time	Memory
1	16.18	303.33		15.57	127.85	
0.1	35.73	206.84	572	35.43	44.48	0.53
0.01	39.56	377.80		38.38	290.56	

SNR (in dB), computation time (in s) and memory storage (in MB) for the restoration of signal A for various values of noise level. Block-circulant approximation $\overline{\mathbf{D}}$ is tested for L = 10.

- Good quality reconstruction even with high noise level.
- ► Block-circulant approximation is faster than exact dictionary approach with limited deterioration of the results quality.



Influence of L?



SNR of the restored signal A with $\sigma = 10^{-2}$ using \overline{D} for various L values

▶ Reconstruction quality stable to the value of *L*.

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Experimental results

Parameters dataset

- peptide EVEALEKKVAALESKVQALEKKVEALEHG-NH2
- 3 μM (C₁₄₀H₂₄₀N₃₈O₄₅).
- \bullet Trimer form within 50 mM of $\rm NH_4OAc$
- BRUKER Solarix 15 T, FT-ICR instrument, ESI source.
- *N* = 8000000

Parameters algorithm

- σ : estimated from an empty frame of the measured signal.
- maximum iterations number : 2000



Experimental results



Analysis of the real FT-ICR MS spectrum of peptide in trimer form : (top) acquired data, (bottom) recovered spectrum z = 5 using block-circulant approximated dictionary with L = 10



MS spectrum analysis



- Theoretical monoisotopic mass of the peptide : m = 9526.337 Daltons.
- Theoretical position of the Sodium : m = +21.982 Daltons.

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Conclusion & perspectives

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Conclusion & perspectives

 \checkmark New dictionary-based approach for MS data analysis based on proteomic averagine model.

 \checkmark Penalized cost function promoting sparsity and positivity, minimized with efficient primal-dual scheme with sought convergence guarantees.

 \checkmark Block-circulant approximation of the dictionary-based approach.

- \Rightarrow Efficient analysis of synthetic and real MS spectra.
- \Rightarrow Fast approach devoted to the big data scale.
- \Rightarrow Limited memory resources required.

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Conclusion & perspectives

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► Extend this approach to the processing of multidimensional MS spectra.

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Thank you for your attention !

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