

# CO $\ell_0$ RME

## COvariance-based $\ell_0$ super-Resolution Microscopy with intensity Estimation

Vasiliki Stergiopoulou, José Henrique de Moraes Goulart, Sébastien Schaub, Luca Calatroni, Laure Blanc-Féraud



Design a sparsity-promoting mathematical model for Super-Resolution in Fluorescence Microscopy.

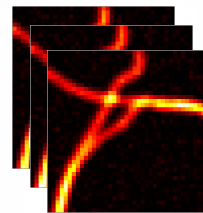


Acquire **short videos** with **high-density** of molecules per frame and use a reconstruction algorithm that codifies the assumption of the **temporal/spatial independence** between emitters and the **sparse distribution** of the fluorescent molecules

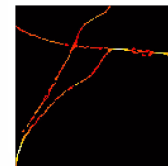
### Features:

- ❖ Improved temporal/spatial resolution
- ❖ Harmless excitation levels
- ❖ Use of standard equipment
- ❖ Intensity estimation

Raw Data



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Two steps:

## Support Estimation:

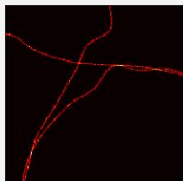


- ❖ Non-convex variational problem with a sparsity constraint formulated in the covariance domain
- ❖ Enforce Sparsity: Continuous Exact  $\ell_0$  Relaxation (CEL0)

$$\Phi_{\text{CEL0}}(\mathbf{r}_\mathbf{x}; \lambda) = \sum_{i=1}^{L^2} \lambda \frac{\|\mathbf{a}_i\|^2}{2} \left( \left| (\mathbf{r}_\mathbf{x})_i \right| - \frac{\sqrt{2\lambda}}{\|\mathbf{a}_i\|} \right) \mathbb{1}_{\{ |(\mathbf{r}_\mathbf{x})_i| \leq \frac{\sqrt{2\lambda}}{\|\mathbf{a}_i\|} \}}$$

, where  $\mathbf{a}_i = (\Psi \circ \Psi)_i$

## Intensity Estimation:



- ❖ Estimate intensity, **only on the support**, and background information
- ❖ Smoothness is promoted on intensity values

**CO $\ell_0$ RME**: Good localization and reconstruction results!